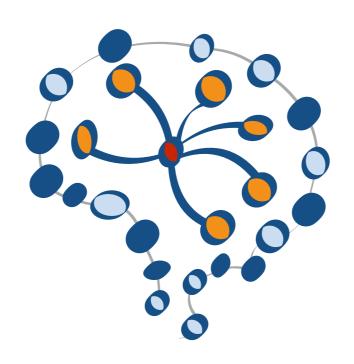
STAT 453: Introduction to Deep Learning and Generative Models

Sebastian Raschka
http://stat.wisc.edu/~sraschka/teaching



Lecture 06

Automatic Differentiation with PyTorch

Today

Computing partial derivatives more easily (and automatically) with PyTorch

Lecture Overview

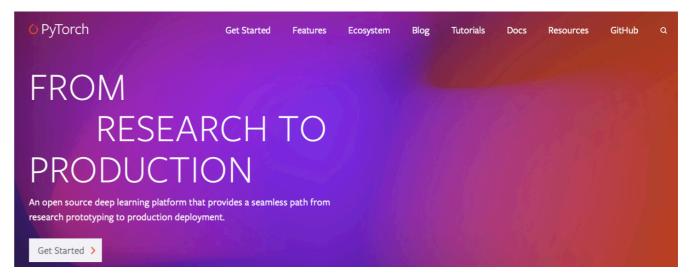
- 1. PyTorch Resources
- 2. Computation Graphs
- 3. Automatic Differentiation in PyTorch
- 4. Training ADALINE Manually Vs Automatically in PyTorch
- 5. A Closer Look at the PyTorch API

Learning More About PyTorch

1. PyTorch Resources

- 2. Computation Graphs
- 3. Automatic Differentiation in PyTorch
- 4. Training ADALINE Manually Vs Automatically in PyTorch
- 5. A Closer Look at the PyTorch API



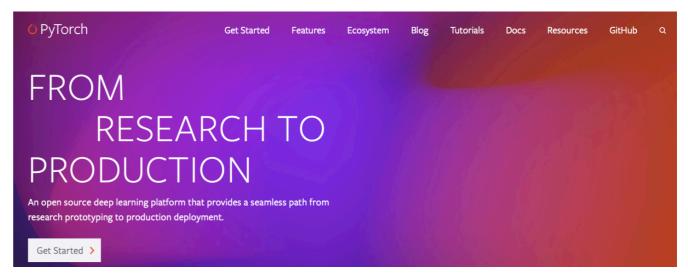


https://pytorch.org/

At a Glance:

- Based on Torch 7, which was based on Lua and inspired by Lush
- PyTorch started in 2016
- Focuses on flexibility and minimizing cognitive overhead
- Dynamic nature of autograd API inspired by Chainer
- Core features
 - Automatic differentiation
 - Dynamic computation graphs
 - NumPy integration
- written in C++ and CUDA (CUDA is like C++ for the GPU)
- Python is the usability glue





https://pytorch.org/

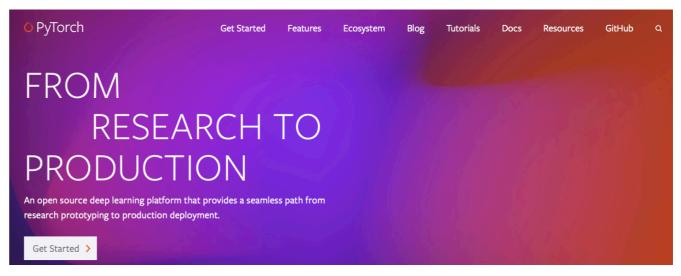
At a Glance:

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- Core features
 - Automatic differentiation
 - Dynamic computation graphs
 - NumPy integration
- written in C++ and CUDA (CUDA is
- Python is the usability glue

PyTorch vs NumPy

- Support GPU
- distribute ops across multiple devices
- keep track of computation graph and ops that created them





https://pytorch.org/

At a Glance:

- Based on Torch 7, which was based on Lua and inspired by Lush
- PyTorch started in 2016
- Focuses on flexibility and minimizing cognitive overhead
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 - Automatic differentiation

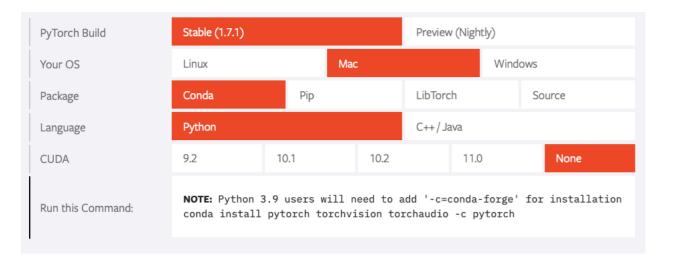
"the speedup gained by taking Python out of the computation is 10% or less" -- Stevens *et al.*: Deep Learning with PyTorch

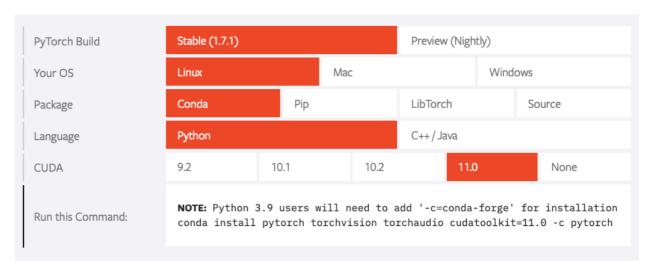
- written in C++ and CUDA (CUDA is like C++ for the GPU)
- Python is the usability glue

Installation

Recommendation for Laptop (e.g., MacBook)

Recommendation for Desktop (Linux) with GPU





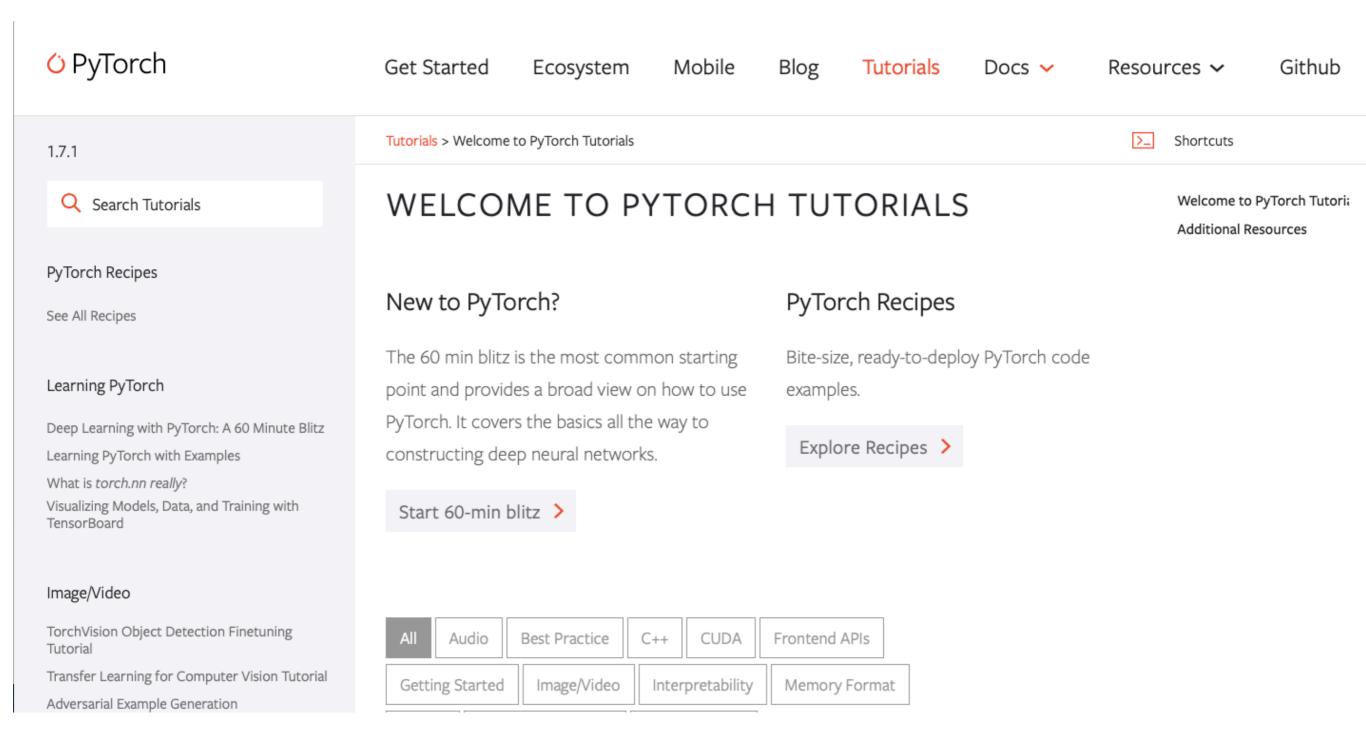
https://pytorch.org/

As mention in the installation tips on Canvas

And don't forget that you import PyTorch as "import torch," not "import pytorch":)

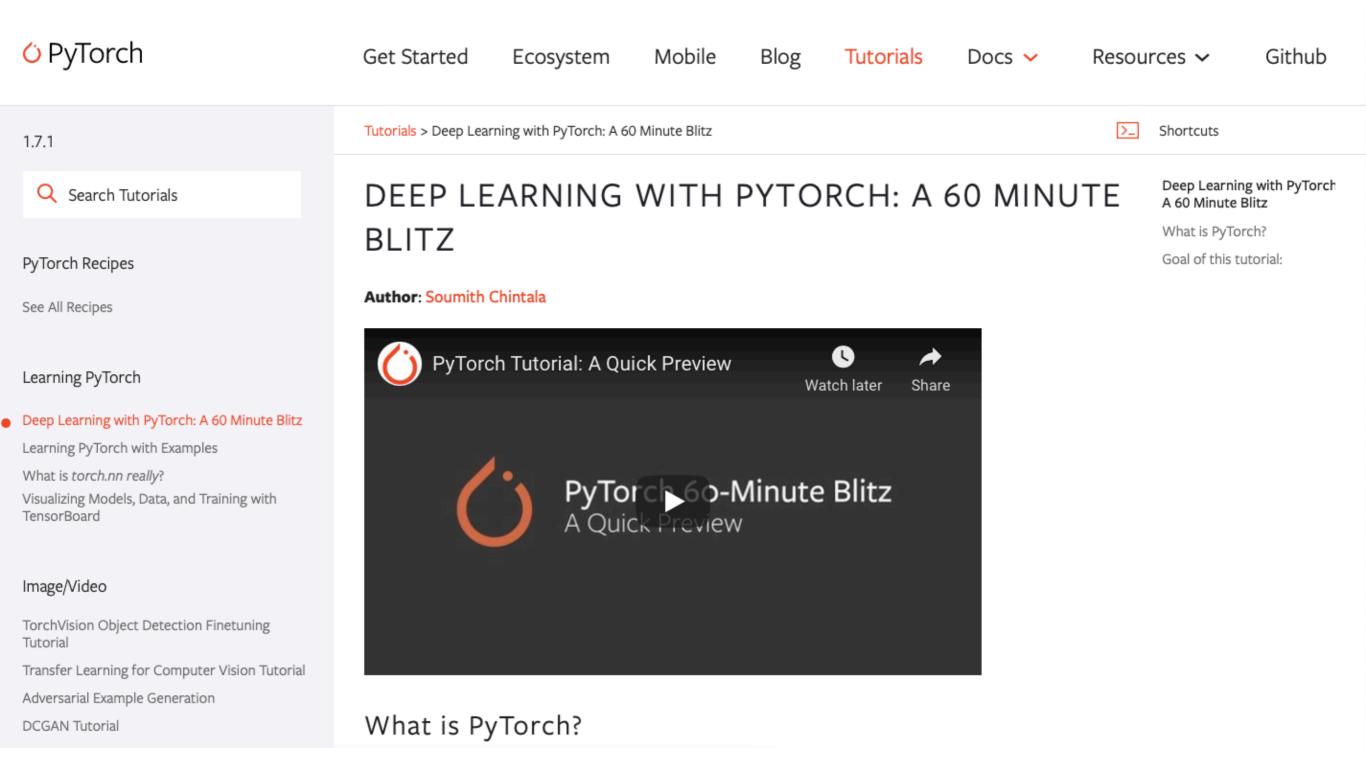
```
[In [1]: import torch
[In [2]: torch.__version__
Out[2]: '1.7.0'
In [3]:
```

Many Useful Tutorials (recommend that you read some of them)

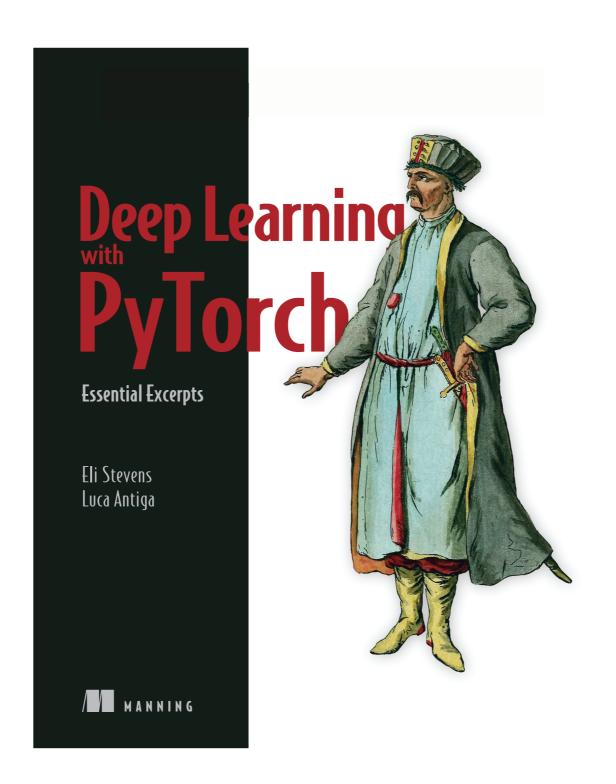


https://pytorch.org/tutorials/

Many Useful Tutorials (recommend that you read some of them)



https://pytorch.org/tutorials/beginner/deep learning 60min blitz.html



https://pytorch.org/assets/deep-learning/Deep-Learning-with-PyTorch.pdf

Very Active & Friendly Community and Help/Discussion Forum





Do you want live notifications when people reply to your posts? Enable Notifications				×
all categories ▶ all ▼ Latest New (47) Unread (104) Top Categories			+ New Topic	
Торіс		Replies	Views	Activity
☑ Using MSELoss instead of CrossEntropy for Ordinal Regression/Classification ■ vision	9 9	2	83	1h
Optimizer.load_state_dict() weird behaviour with Adam optimizer vision	A 🔮 🚇 🍩	7	2.0k	1h
Is there a way to train 3 dataloaders using multiprocessing? •	재민	0	11	2h
 ☑ Getting different feature vectors from frozen layers after training ■ vision 	S	5	86	2h
□ Libtorch_cuda.so is too large (>2GB) □ deployment	9 👰 🚱	22	346	2h
Undo pruning - How to 'unmask' pruned weights ■ vision	8	0	8	2h
If input.dim() == 2 and bias is not None: AttributeError: 'tuple' object has no attribute 'dim •		3	41	2h
Export unsupported/compound ops to ONNX • deployment	G	0	9	2h

https://discuss.pytorch.org

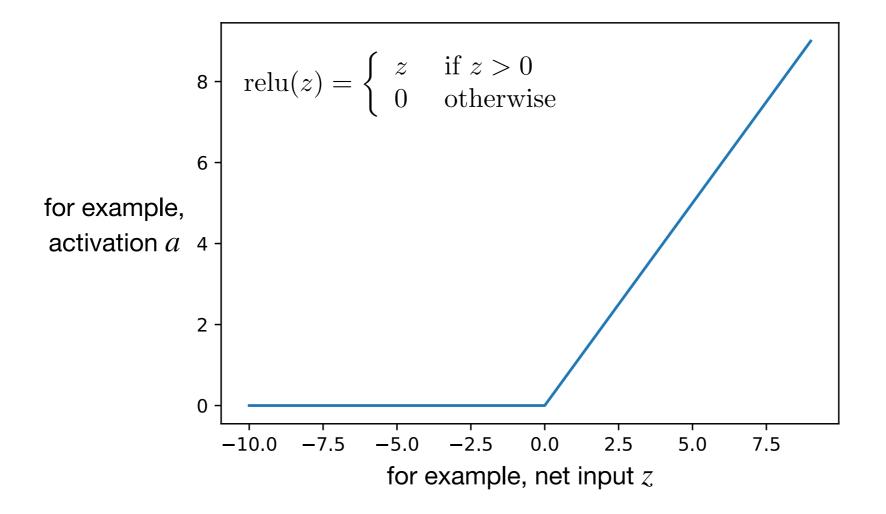
Understanding Automatic Differentiation via Computation Graphs

- 1. PyTorch Resources
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In the context of deep learning (and PyTorch) it is helpful to think about neural networks as computation graphs

Suppose we have the following activation function:

$$a(x, w, b) = relu(w \cdot x + b)$$



ReLU = Rectified Linear Unit

(prob. the most commonly used activation function in DL)

Side-note about ReLU Function

You may note that

$$\sigma'(z) = \begin{cases} 0 & \text{if } z < 0 \\ 1 & \text{if } z > 0 \\ \text{DNE} & \text{if } z = 0 \end{cases}$$

But in the machine learning--computer science context, for convenience, we can just say

$$\sigma'(z) = \begin{cases} 0 & \text{if } z \le 0\\ 1 & \text{if } z > 0 \end{cases}$$

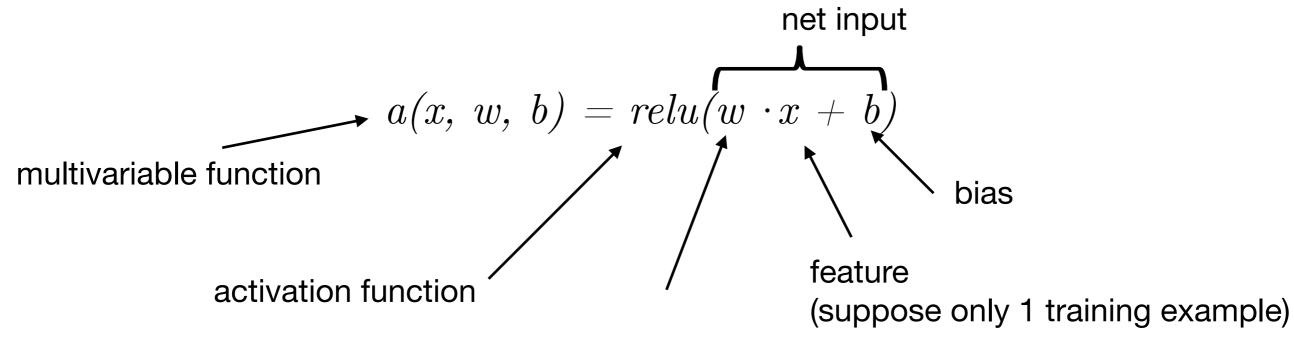
Why not differentiable? Derivative does not exist (DNE) at 0, because the derivative is different if we approach the limit from the left or right:

$$\sigma'(z) = \lim_{z \to 0} \frac{\max(0, z + \Delta z) - \max(0, z)}{\Delta z}$$

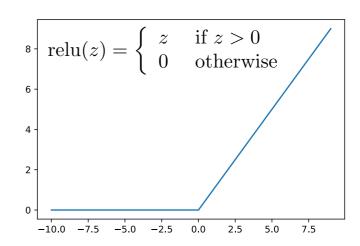
$$\sigma'(0) = \lim_{z \to 0^+} \frac{0 + \Delta z - 0}{\Delta z} = 1$$

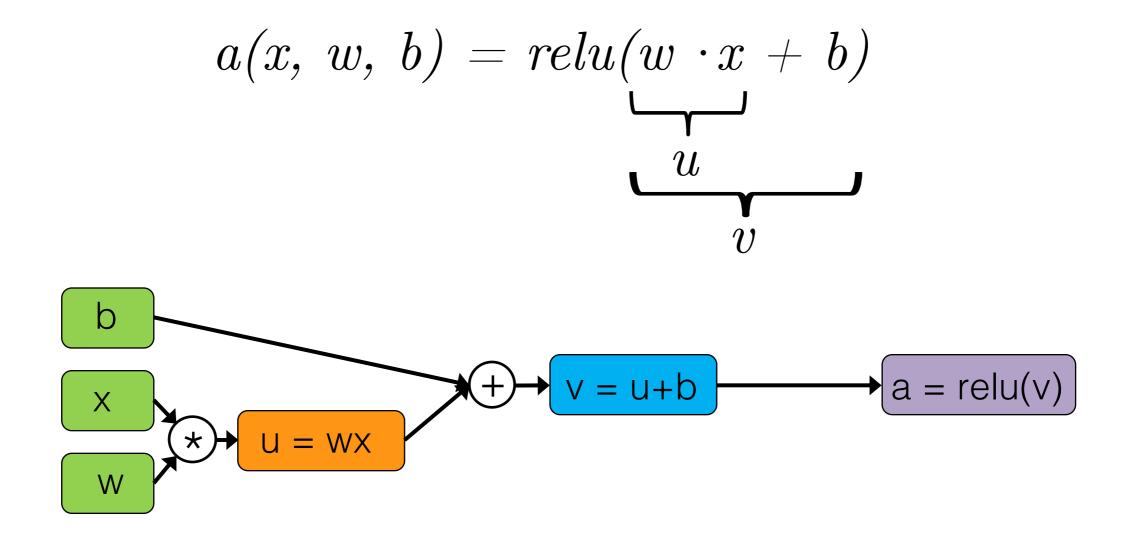
$$\sigma'(0) = \lim_{z \to 0^{-}} \frac{0 - 0}{\Delta z} = 0$$

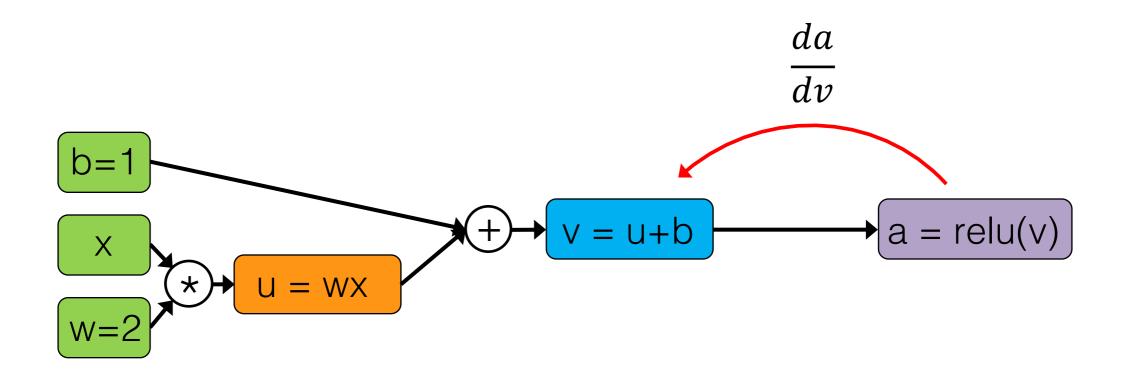
Suppose we have the following activation function:

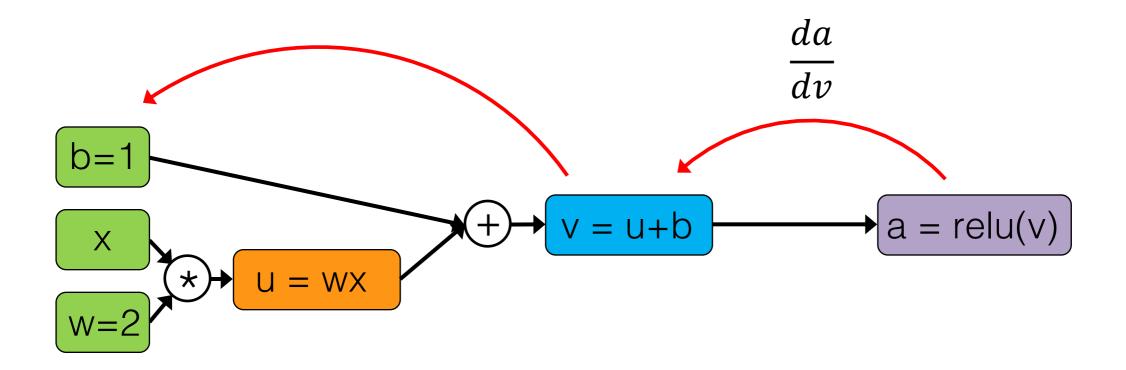


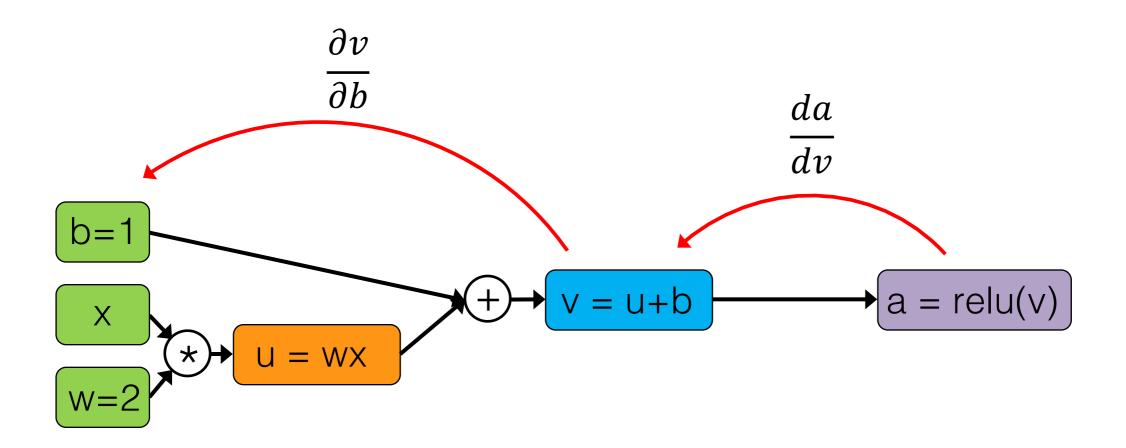
weight parameter (assume only 1 input feature)

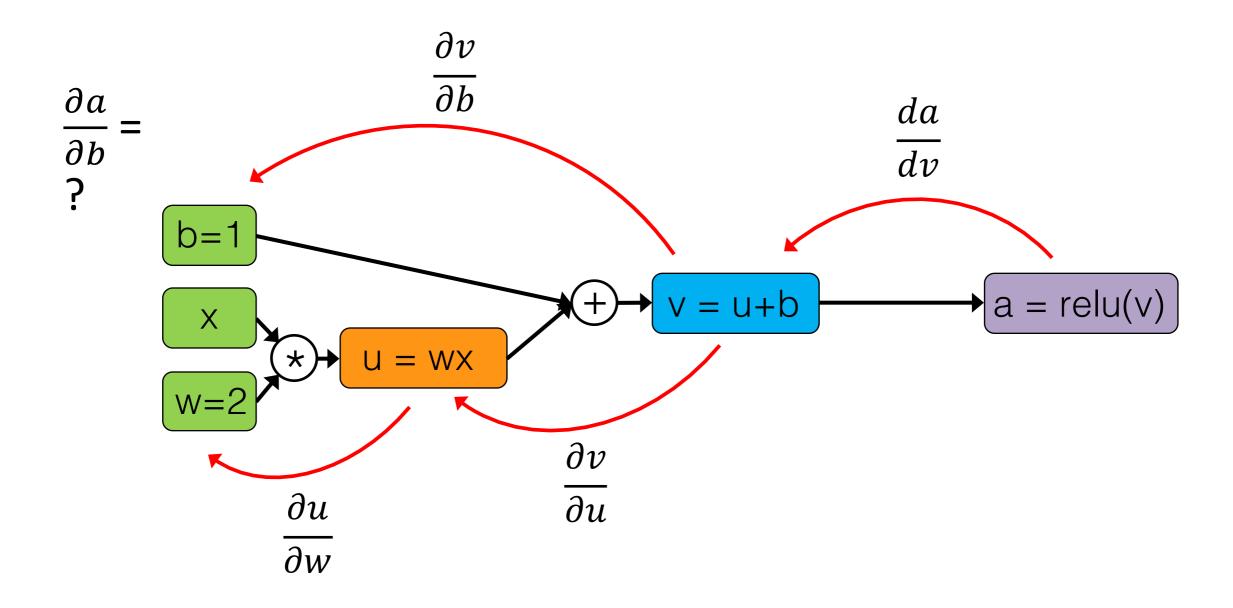


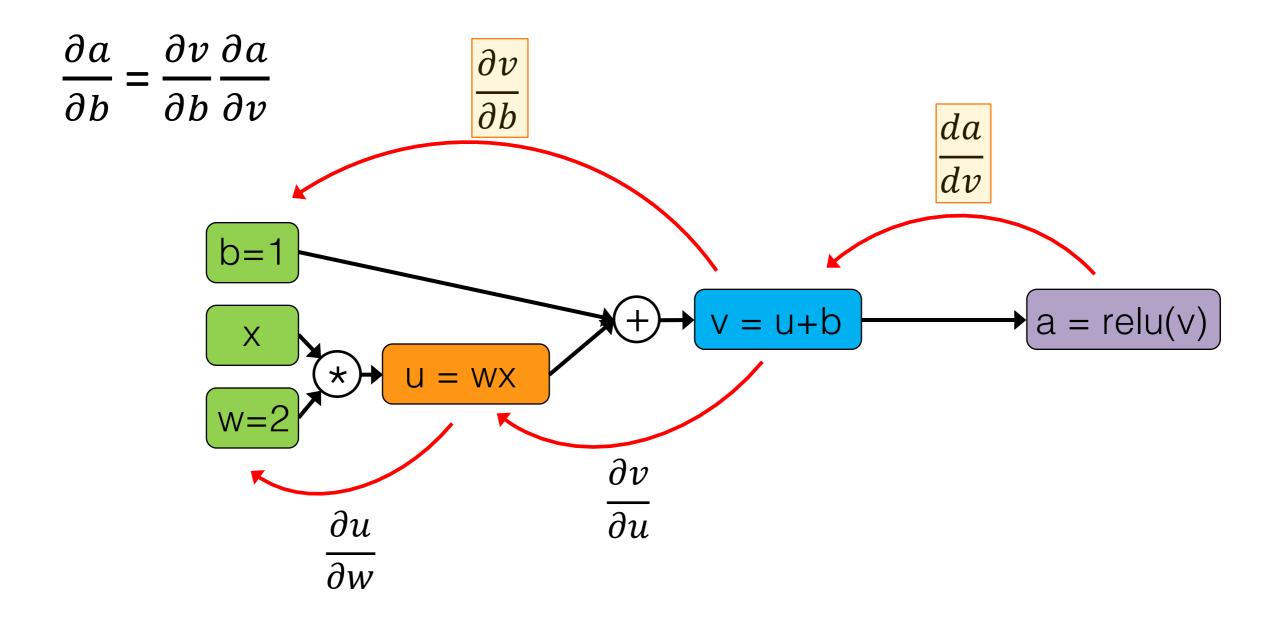


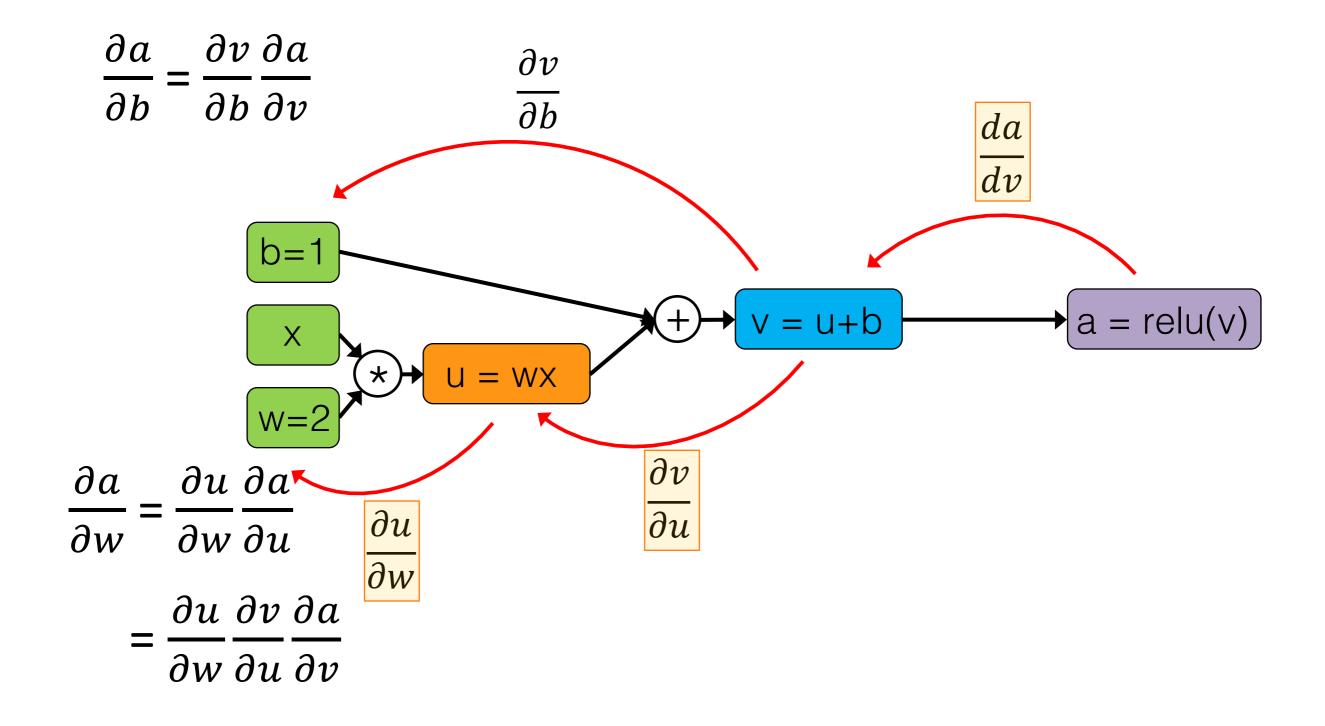


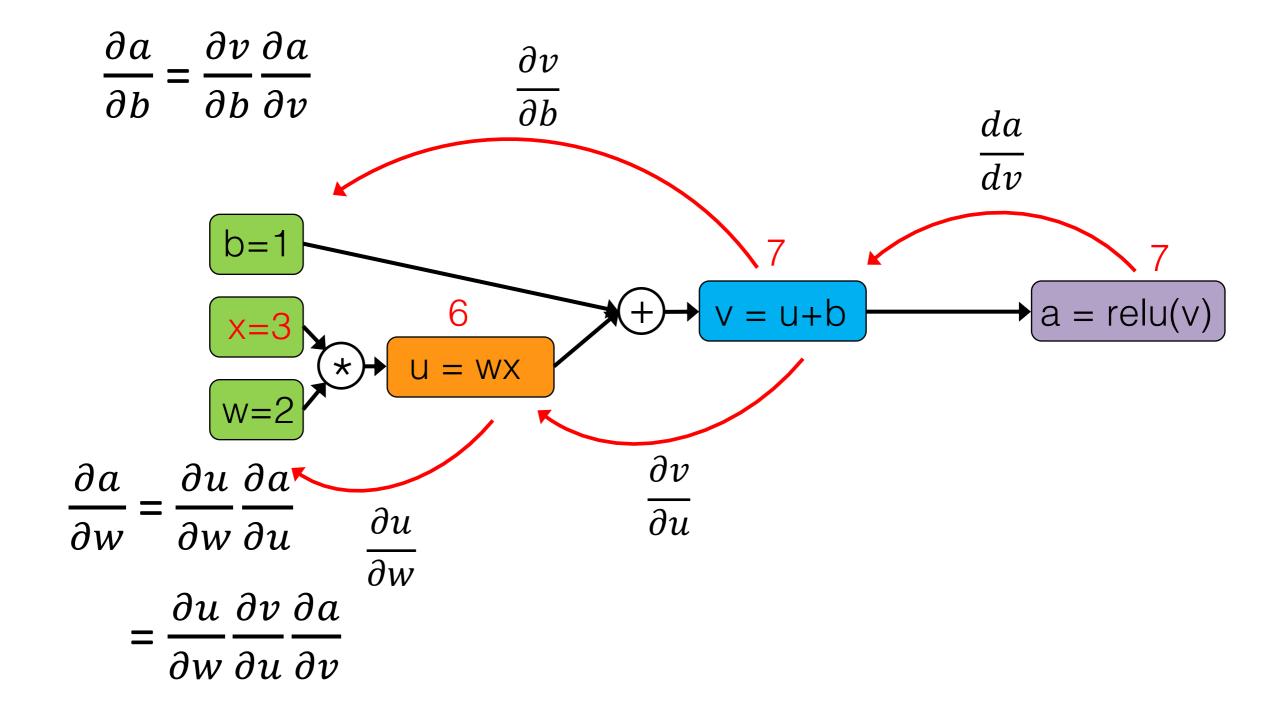


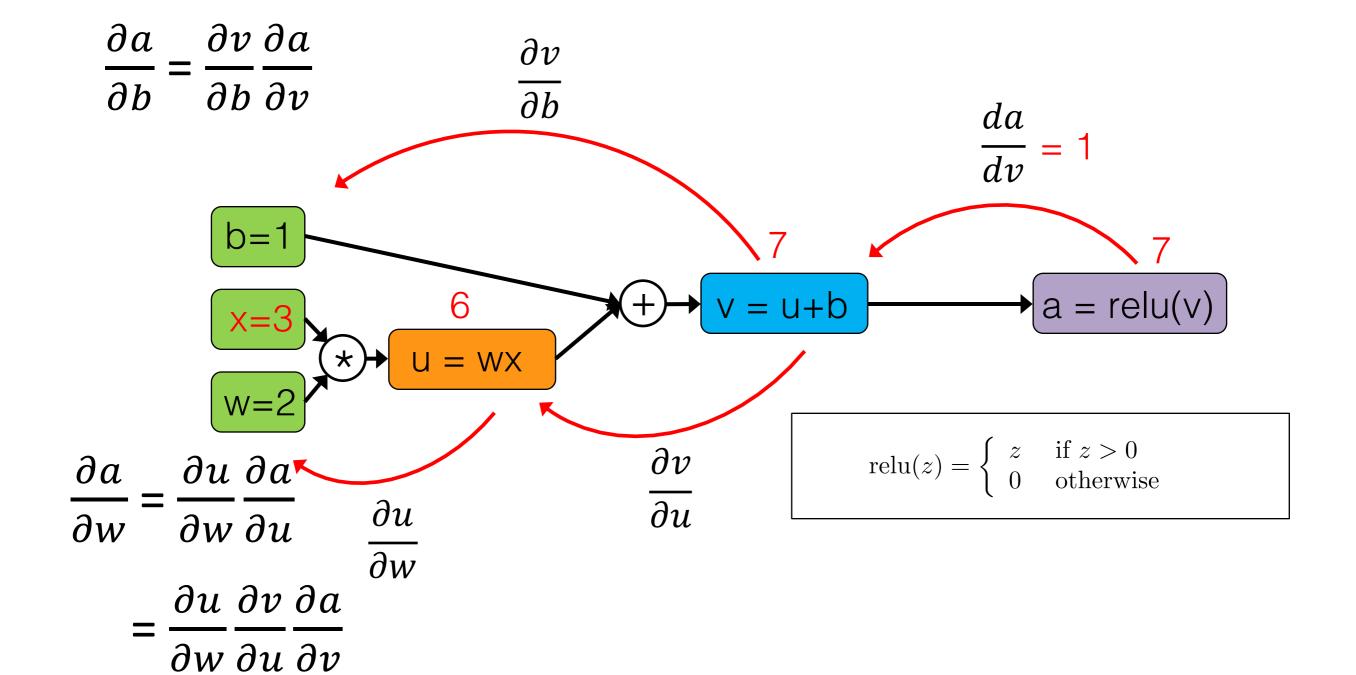


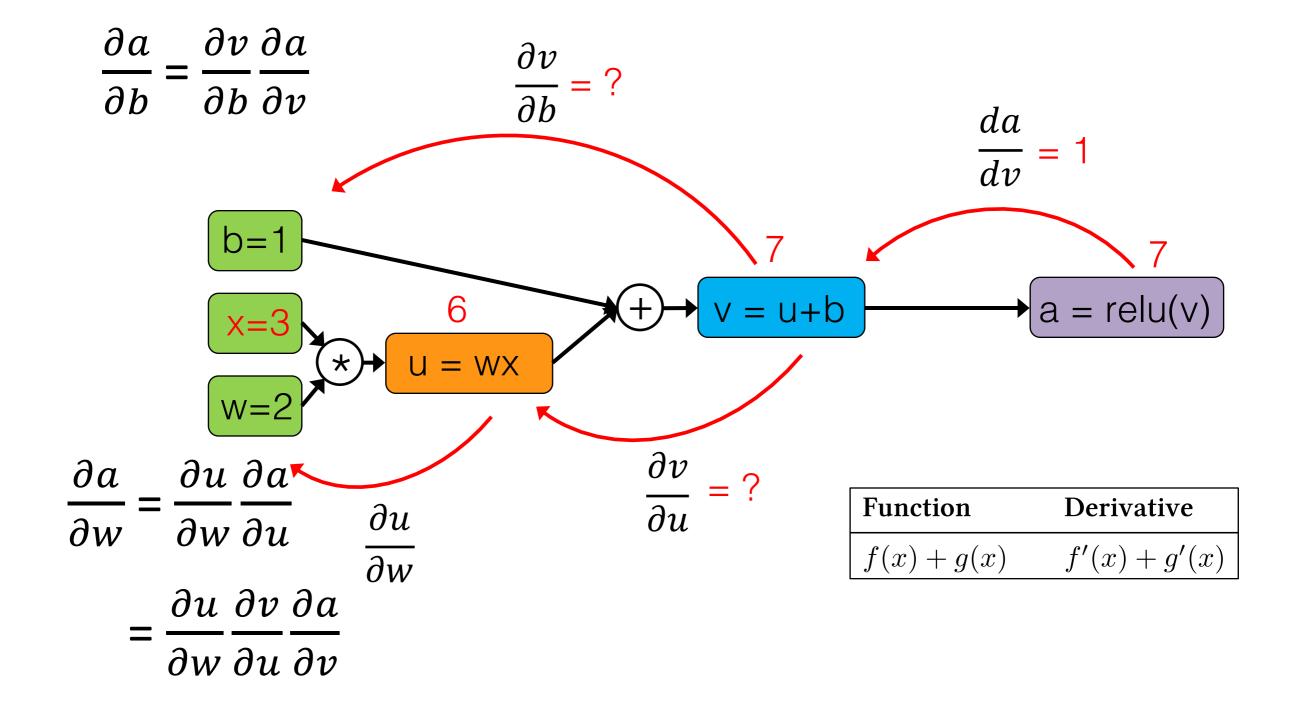


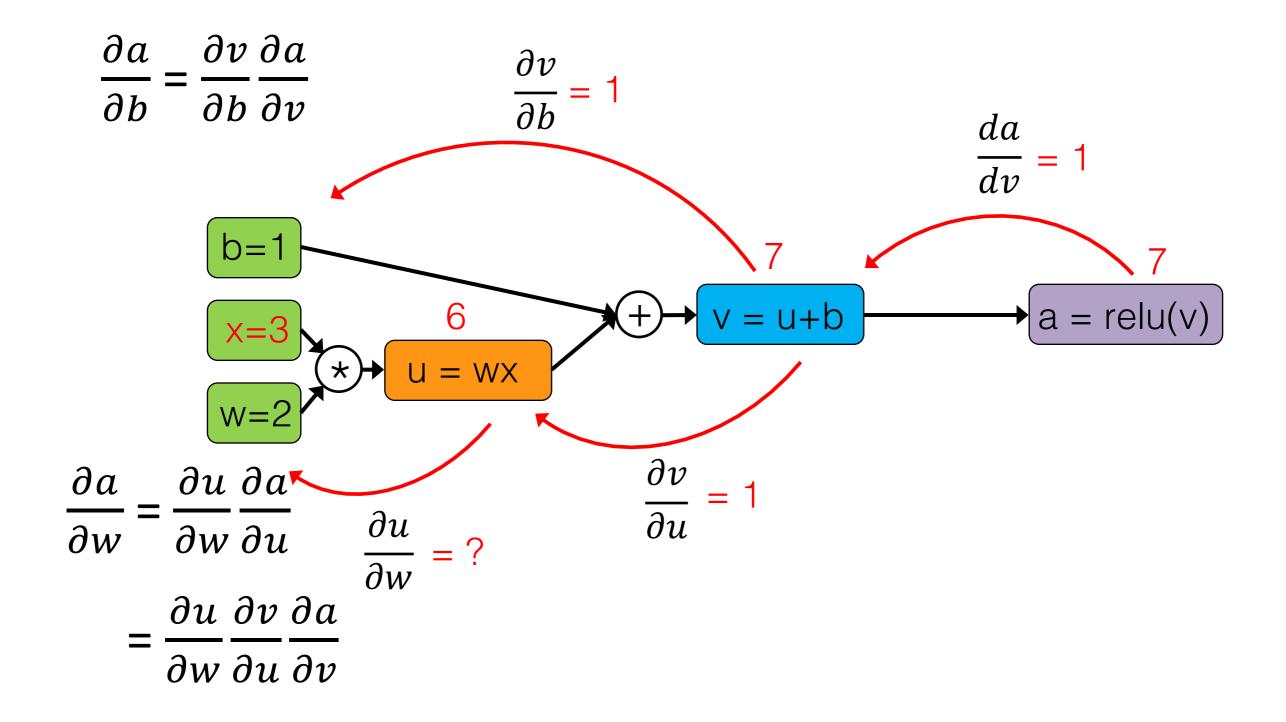


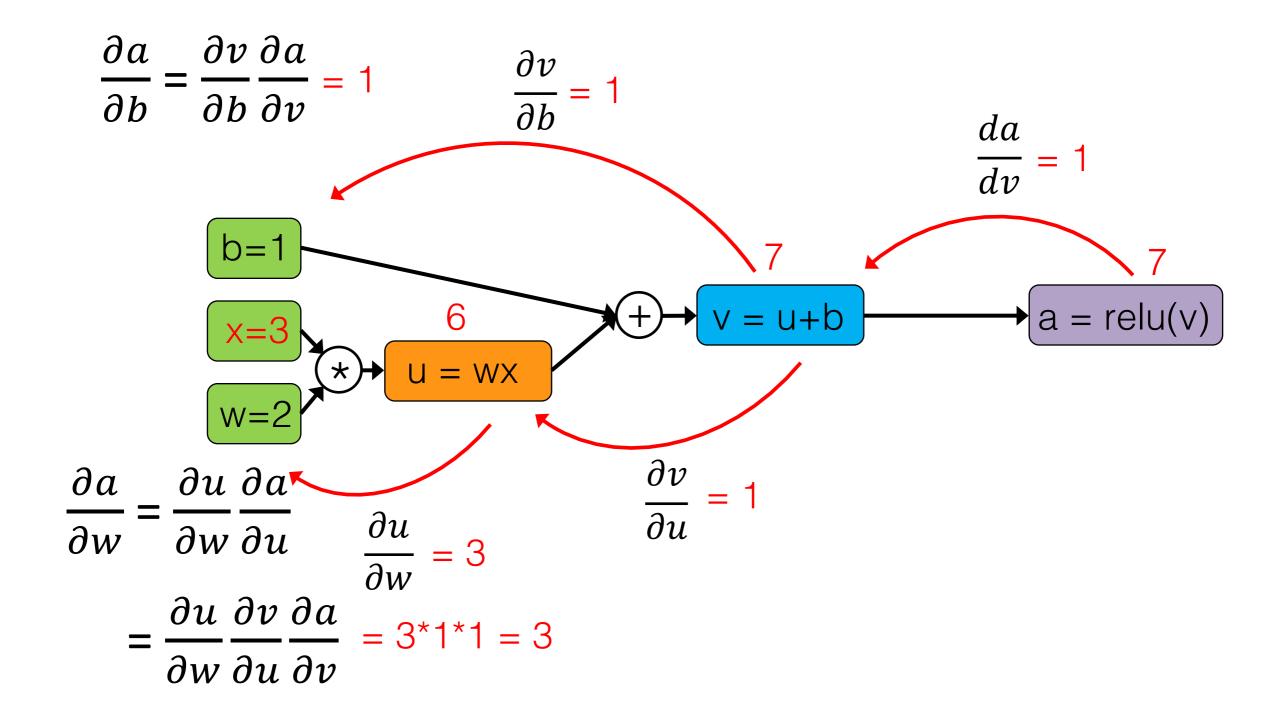












Some More Computation Graphs

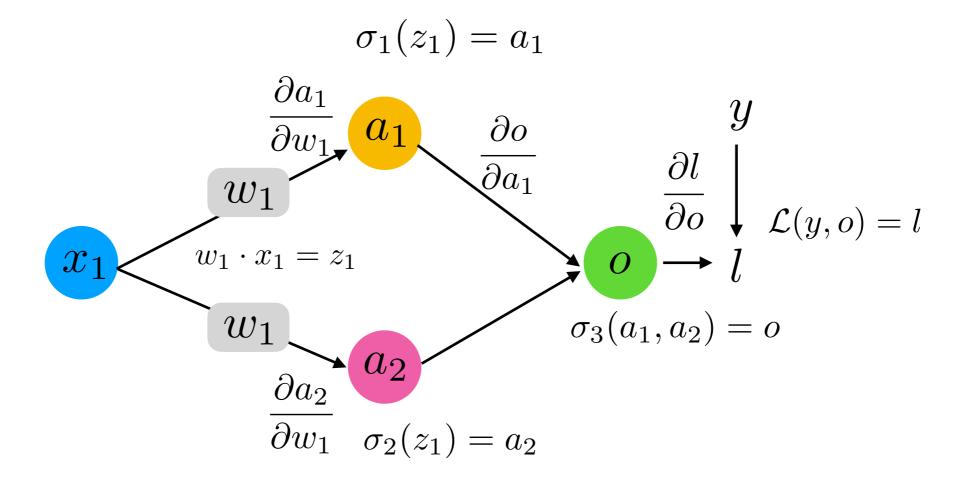
Graph with Single Path

$$\mathcal{L}(y, \sigma_1(w_1 \cdot x_1))$$
 $x_1 \longrightarrow w_1 \longrightarrow a_1 \longrightarrow o \longrightarrow l$
 y
 $\mathcal{L}(y, o) = l$
 y
 $\mathcal{L}(y, o) = l$

$$\frac{\partial l}{\partial w_1} = \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_1} \cdot \frac{\partial a_1}{\partial w_1} \quad \text{(univariate chain rule)}$$

Graph with Weight Sharing

$$\mathcal{L}(y,\sigma_3[\sigma_1(w_1\cdot x_1),\sigma_2(w_1\cdot x_1)])$$

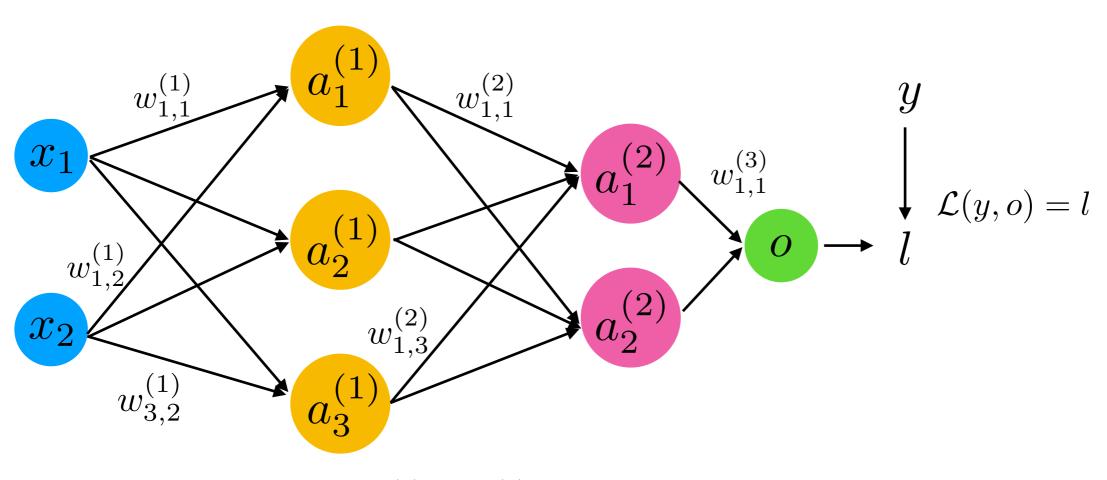


Upper path

$$\frac{\partial l}{\partial w_1} = \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_1} \cdot \frac{\partial a_1}{\partial w_1} + \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_2} \cdot \frac{\partial a_2}{\partial w_1} \quad \text{(multivariable chain rule)}$$

Lower path

Graph with Fully-Connected Layers (later in this course)



$$\frac{\partial l}{\partial w_{1,1}^{(1)}} = \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_1^{(2)}} \cdot \frac{\partial a_1^{(2)}}{\partial a_1^{(1)}} \cdot \frac{\partial a_1^{(1)}}{\partial w_{1,1}^{(1)}} + \frac{\partial l}{\partial o} \cdot \frac{\partial o}{\partial a_2^{(2)}} \cdot \frac{\partial a_2^{(2)}}{\partial a_1^{(2)}} \cdot \frac{\partial a_2^{(1)}}{\partial a_1^{(1)}} \cdot \frac{\partial a_1^{(1)}}{\partial w_{1,1}^{(1)}} + \frac{\partial a_1^{(1)}}{\partial w_{1,1}^{(1)}}$$

Automatic Differentiation with PyTorch

-- An Autograd Example

- 1. PyTorch Resources
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PyTorch Autograd Example

https://github.com/rasbt/stat453-deep-learning-ss21/tree/master/L06/code/pytorch-autograd.ipynb

Training an Adaptive Linear Neuron in PyTorch

- 1. PyTorch Resources
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simplify to super().__init__() in constructor

PyTorch ADALINE (neuron model) Example

https://github.com/rasbt/stat453-deep-learning-ss21/tree/master/L06/code/adaline-with-autograd.ipynb

Using PyTorch: A Closer Look at the Object-Oriented and Functional APIs

- 1. PyTorch Resources
- 2. Computation Graphs
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PyTorch Usage: Step 1 (Definition)

```
class MultilayerPerceptron(torch.nn.Module):
    def init (self, num features, num classes):
        super(MultilayerPerceptron, self). init ()
        ### 1st hidden layer
        self.linear 1 = torch.nn.Linear(num feat, num h1)
       ### 2nd hidden layer
        self.linear 2 = torch.nn.Linear(num h1, num h2)
        ### Output layer
        self.linear out = torch.nn.Linear(num h2, num classes)
    def forward(self, x):
        out = self.linear 1(x)
        out = F.relu(out)
        out = self.linear 2(out)
        out = F.relu(out)
        logits = self.linear out(out)
        probas = F.log softmax(logits, dim=1)
```

return logits, probas

Backward will be inferred automatically if we use the nn.Module class!

Define model parameters that will be instantiated when created an object of this class

Define how and it what order the model parameters should be used in the forward pass

PyTorch Usage: Step 2 (Creation)

PyTorch Usage: Step 2 (Creation)

```
Run for a specified number of
                                            epochs
                                                                           Iterate over minibatches
for epoch in range(num epochs):
                                                                           in epoch
    model.train()
     for batch idx, (features, targets) in enumerate(train loader):
                                                                           If your model is on the
         features = features.view(-1, 28*28).to(device)
                                                                           GPU, data should also
         targets = targets.to(device)
                                                                           be
         ### FORWARD AND BACK PROP
                                                                           on the GPU
         logits, probas = model(features)
         cost = F.cross entropy(probas, targets)
         optimizer.zero grad()
         cost.backward()
                                                               y = model(x) calls . call and then .forward(), where some
                                                               extra stuff is done in call;
         ### UPDATE MODEL PARAMETERS
                                                               don't run y = model.forward(x) directly
         optimizer.step()
    model.eval()
    with torch.no grad():
                                      Gradients at each leaf node are accumulated under the .grad attribute, not just stored. This is why we
         # compute accuracy
                                      have to zero them before each backward pass
```

```
for epoch in range(num epochs):
    model.train()
    for batch idx, (features, targets) in enumerate(train loader):
         features = features.view(-1, 28*28).to(device)
        targets = targets.to(device)
        ### FORWARD AND BACK PROP
         logits, probas = model(features)
This will run the forward() method
         loss = F.cross_entropy(logits, targets)← Define a loss function to optimize
         optimizer.zero_grad() ← Set the gradient to zero
                                         (could be non-zero from a previous forward pass)
         loss.backward()
                                          Compute the gradients, the backward is
        ### UPDATE MODEL PARAMETERS
                                          automatically constructed by "autograd" based on
         optimizer.step()
                                          the forward() method and the loss function
                                            Use the gradients to update the weights according to
    model.eval()
    with torch.no grad():
                                            the optimization method (defined on the previous
        # compute accuracy
                                            slide)
                                            E.g., for SGD, w := w + \text{learning} rate \times gradient
```

```
for epoch in range(num epochs):
    model.train()
    for batch idx, (features, targets) in enumerate(train loader):
        features = features.view(-1, 28*28).to(device)
        targets = targets.to(device)
        ### FORWARD AND BACK PROP
        logits, probas = model(features)
        loss = F.cross entropy(logits, targets)
        optimizer.zero grad()
        loss.backward()
        ### UPDATE MODEL PARAMETERS
        optimizer.step()
                                      For evaluation, set the model to eval mode (will be
                                      relevant later when we use DropOut or BatchNorm)
    model.eval()
    with torch.no grad():
        # compute accuracy
                                            This prevents the computation graph for
                                            backpropagation from automatically being build in
                                            the background to save memory
```

```
for epoch in range(num epochs):
    model.train()
    for batch idx, (features, targets) in enumerate(train loader):
        features = features.view(-1, 28*28).to(device)
        targets = targets.to(device)
        ### FORWARD AND BACK PROP
        logits, probas = model(features)
        loss = F.cross entropy(logits, targets)
        optimizer.zero grad()
        loss.backward()
                                         logits because of computational efficiency.
        ### UPDATE MODEL PARAMETERS
                                         Basically, it internally uses a log softmax(logits) function
        optimizer.step()
                                         that is more stable than log(softmax(logits)).
                                         More on logits ("net inputs" of the last layer) in the
    model.eval()
                                         next lecture. Please also see
    with torch.no grad():
        # compute accuracy
```

Objected-Oriented vs Functional* API

*Note that with "functional" I mean "functional programming" (one paradigm in CS) torch.nn.functional = api without internal state

```
import torch.nn.functional as F
class MultilayerPerceptron(torch.nn.Module):
    def init (self, num features, num classes):
        super(MultilayerPerceptron, self). init ()
       ### 1st hidden layer
        self.linear 1 = torch.nn.Linear(num features,
                                       num hidden 1)
       ### 2nd hidden layer
        self.linear 2 = torch.nn.Linear(num hidden 1,
                                       num hidden 2)
       ### Output layer
        self.linear out = torch.nn.Linear(num hidden 2,
                                          num classes)
    def forward(self, x):
       out = self.linear 1(x)
       out = F.relu(out)
       out = self.linear 2(out)
       out = F.relu(out)
       logits = self.linear out(out)
       probas = F.log softmax(logits, dim=1)
       return logits, probas
            Unnecessary because these functions
            don't need to store a state but maybe
            helpful for keeping track of order of ops
```

(when implementing "forward")

```
class MultilayerPerceptron(torch.nn.Module):
    def init (self, num features, num classes):
        super(MultilayerPerceptron, self). init ()
        ### 1st hidden layer
        self.linear 1 = torch.nn.Linear(num features,
                                        num hidden 1)
        self.relu1 = torch.nn.ReLU()
        ### 2nd hidden layer
       self.linear 2 = torch.nn.Linear(num hidden 1,
                                        num hidden 2)
        self.relu2 = torch.nn.ReLU()
        ### Output layer
        self.linear out = torch.nn.Linear(num hidden 2,
                                          num classes)
        self.softmax = torch.nn.Softmax()
    def forward(self, x):
        out = self.linear 1(x)
        out = self.relu1(out)
        out = self.linear 2(out)
        out = self.relu2(out)
        logits = self.linear out(out)
       probas = self.softmax(logits, dim=1)
        return logits, probas
```

Objected-Oriented vs Functional API

Using "Sequential"

```
import torch.nn.functional as F
class MultilayerPerceptron(torch.nn.Module):
                                                              class MultilayerPerceptron(torch.nn.Module):
    def init (self, num features, num classes):
                                                                  def __init__(self, num features, num classes):
        super(MultilayerPerceptron, self). init ()
                                                                      super(MultilayerPerceptron, self). init ()
        ### 1st hidden layer
                                                                      self.my network = torch.nn.Sequential(
        self.linear 1 = torch.nn.Linear(num features,
                                                                          torch.nn.Linear(num features, num hidden 1),
                                        num hidden 1)
                                                                          torch.nn.ReLU(),
                                                                          torch.nn.Linear(num hidden 1, num hidden 2),
       ### 2nd hidden layer
                                                                          torch.nn.ReLU(),
        self.linear 2 = torch.nn.Linear(num hidden 1,
                                                                          torch.nn.Linear(num hidden 2, num classes)
                                        num hidden 2)
        ### Output layer
                                                                  def forward(self, x):
        self.linear out = torch.nn.Linear(num_hidden_2,
                                                                      logits = self.my network(x)
                                          num classes)
                                                                      probas = F.softmax(logits, dim=1)
                                                                      return logits, probas
    def forward(self, x):
        out = self.linear 1(x)
                                                                      Much more compact and clear, but
        out = F.relu(out)
                                                                      "forward" may be harder to debug if there
        out = self.linear 2(out)
        out = F.relu(out)
                                                                      are errors (we cannot simply add
       logits = self.linear out(out)
                                                                      breakpoints or insert "print" statements
        probas = F.log softmax(logits, dim=1)
        return logits, probas
```

Objected-Oriented vs Functional API

Using "Sequential"

```
1)
   class MultilayerPerceptron(torch.nn.Module):
       def init (self, num features, num classes):
           super(MultilayerPerceptron, self). init ()
           self.my network = torch.nn.Sequential(
               torch.nn.Linear(num features, num hidden
               torch.nn.ReLU(),
               torch.nn.Linear(num hidden 1, num hidden
               torch.nn.ReLU(),
               torch.nn.Linear(num hidden 2, num classe
       def forward(self, x):
           logits = self.my network(x)
           probas = F.softmax(logits, dim=1)
           return logits, probas
        Much more compact and clear, but
        "forward" may be harder to debug if there
        are errors (we cannot simply add
```

breakpoints or insert "print" statements

However, if you use Sequential, you can 2) define "hooks" to get intermediate outputs. For example:

```
[7]: model.net
     Sequential(
       (0): Linear(in_features=784, out_features=128, bias=True)
       (1): ReLU(inplace)
       (2): Linear(in_features=128, out_features=256, bias=True)
       (3): ReLU(inplace)
        (4): Linear(in_features=256, out_features=10, bias=True)
     If we want to get the output from the 2nd layer during the forward pass, we can register a hook as follows:
[8]: outputs = []
     def hook(module, input, output):
         outputs.append(output)
     model.net[2].register_forward_hook(hook)
     <torch.utils.hooks.RemovableHandle at 0x7f659c6685c0>
     Now, if we call the model on some inputs, it will save the intermediate results in the "outputs" list:
      = model(features)
     print(outputs)
     [tensor([[0.5341, 1.0513, 2.3542, ..., 0.0000, 0.0000, 0.0000],
              [0.0000, 0.6676, 0.6620, ..., 0.0000, 0.0000, 2.4056],
              [1.1520, 0.0000, 0.0000, ..., 2.5860, 0.8992, 0.9642],
              [0.0000, 0.1076, 0.0000, ..., 1.8367, 0.0000, 2.5203],
              [0.5415, 0.0000, 0.0000, ..., 2.7968, 0.8244, 1.6335],
              [1.0710, 0.9805, 3.0103, ..., 0.0000, 0.0000, 0.0000]],
            device='cuda:3', grad_fn=<ThresholdBackward1>)]
```

https://github.com/IgorSusmelj/pytorch-styleguide

Jupyter Notebook vs Python Scripts

In general, we recommend to use jupyter notebooks for initial exploration/ playing around with new models and code. Python scripts should be used as soon as you want to train the model on a bigger dataset where also reproducibility is more important.

Our recommended workflow:

- 1. Start with a jupyter notebook
- 2. Explore the data and models
- 3. Build your classes/ methods inside cells of the notebook
- 4. Move your code to python scripts
- 5. Train/ deploy on server

Jupyter Notebook	Python Scripts
+ Exploration	+ Running longer jobs without interruption
+ Debugging	+ Easy to track changes with git
- Can become a huge file	- Debugging mostly means rerunning the whole script
- Can be interrupted (don't use for long training)	
- Prone to errors and become a mess	

Туре	Convention	Example
Packages & Modules	lower_with_under	from prefetch_generator import BackgroundGenerator
Classes	CapWords	class DataLoader
Constants	CAPS_WITH_UNDER	BATCH_SIZE=16
Instances	lower_with_under	dataset = Dataset
Methods & Functions	lower_with_under()	def visualize_tensor()
Variables	lower_with_under	background_color='Blue'

More PyTorch features will be introduced step-bystep later in this course when we start working with more complex networks, including

- Running code on the GPU
- Using efficient data loaders
- Splitting networks across different GPUs